Section A (50 marks)

1. (a) Round off 0.0749618 to 3 significant figures.

Answer (a) [1]

(b) Use a calculator to evaluate $\frac{\sqrt{42} - \left(\frac{11}{3}\right)^2}{0.7\pi + \left(\sqrt[3]{151} - (-2)^3\right)}$, giving your answer correct to 2 decimal places.

Answer (b) [1]

2. Without the use of a calculator, estimate the value of $\frac{17 \div \sqrt{93}}{\sqrt[3]{209} - 4.58}$, giving your answer correct to 1 significant figure.

Answer [2]

3. Study the set of numbers and write down all the **irrational numbers** in the answer space provided.

$$-0.33, -\frac{1}{7}, 0, \sqrt{169}, \pi, \sqrt{0.5}, \sqrt{8}, 1.3, 2^3$$

Answer [1]

4.	Wri	tten as the product of its prime factors,	
		$252 = 2^2 \times 3^2 \times 7.$	
	(a)	Express 630 as the product of its prime factors in index notation.	
		Answer (a)	[1]
	(b)	Find the HCF of 252 and 630. Give your answer as the product of its prime factors in index notation.	
		Answer (b)	[1]
	(c)	Find the smallest possible value of a whole number x if $630x$ is a multiple of 252.	

Answer (c) [2]

5. Simplify the following expressions.

(a)
$$3(x-y)+[5x-(-2x+y)]$$

$$\text{(b)} \quad \frac{(x-2x^2)}{x} - 4x$$

- 6. Factorise the following expressions completely
 - (a) 42ac 7c,

Answer (a) _____ [1]

(b) $5x^2 - 10xy + 15x$.

Answer (b) [1]

- 7. Solve the following equations.
 - (a) 5k+4=-2(k-9)

Answer (a) [2]

(b) $7-n = \frac{-9n+1}{2}$

Answer (b) [3]

8. If $k = \sqrt{\frac{2m}{m-n}}$, find the value of *n* when k = 2 and m = -4.



9. George has \$y and Sam has \$18 more than George. Tim has half the total amount of George and Sam.

Find an expression, in terms of y, for

(a) the amount of money Sam has,

(b) the total amount the 3 of them have together.

10. Without using a calculator and showing your working clearly, evaluate

$$\left(\frac{2}{3} + \frac{3}{4}\right) \times \left(\frac{4}{3} \div \frac{2}{3}\right).$$

- Answer [3]
- 11. The foot of the mountain is at sea level. The temperatures at the foot and at the summit of the mountain are 11° C and -7° C respectively.
 - (a) Find the difference between the two temperatures.

- Answer (a) [1]
- (b) Suppose that the temperature drops by 6°C for every 1000 m above sea level. How high is the mountain above sea level?

Answer (b) [2]

12.

WAFFLES

Write down all the letters in the word above that have

(a) one line of symmetry,

Answer (a)

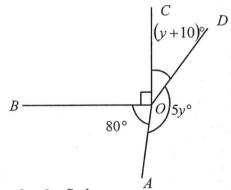
[1]

(b) rotational symmetry of order two.

Answer (b)

[1]

13. In the figure below, OA, OB, OC and OD are all straight lines. $\angle COB = 90^{\circ}$ and $\angle AOB = 80^{\circ}$.



Stating your reasons clearly, find

(a) the value of y,

Answer (a)

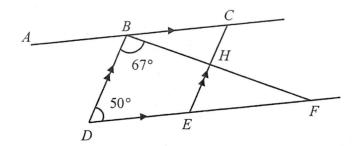
[2]

(b) the obtuse angle AOD.

Answer (b)

[1]

14. In the figure below, ABC, DEF and BHF are straight lines. AC // DF and BD // CE. $\angle DBF = 67^{\circ}$ and $\angle BDF = 50^{\circ}$.



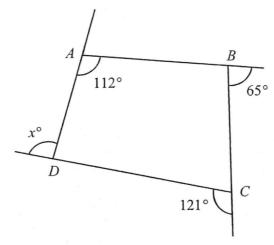
Stating your reasons clearly, find

(a) $\angle BCE$,

(b) $\angle ABD$,

(c) $\angle CBH$.

15. In the diagram below, ABCD is a quadrilateral. $\angle DAB = 112^{\circ}$ while two of its exterior angles are 65° and 121° . Find the value of x.



Answer_

[2]

16.	(a)	In the answer space below, construct a triangle XYZ such that $XY = 9$ cm, $YZ = 10$ cm and $\angle XYZ = 85^{\circ}$. The line XY has already been drawn.	[3]
	(b)	On the same diagram,	
		(i) construct the angle bisector of $\angle XZY$.	[1]
		(ii) construct the perpendicular bisector of YZ.	[1]
	(c)	The point M is the intersection of the two bisectors drawn. Measure and write down the value of obtuse $\angle XMZ$.	

X 9 cm *Y*

Answer (c)

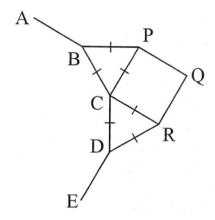
[1]

Section B (30 marks)

Answer all the questions in this section on the writing paper provided.

1	(a)		ctangular board measures 198 cm by 156 cm. It is cut into squares of equal with no material left over.	
		Find		[2]
		(i)	the largest possible length of the side of the square,	[2]
		(ii)	the largest possible area of such a square.	[1]
		(iii)	the number of squares formed.	[1]
	(b)	years	different comets pass through our solar system every 64 years and 216 respectively. The last time they passed through our solar system together n the year 2014. In which year will they next pass through our solar system	
		toget	· · · · · · · · · · · · · · · · · · ·	[3]
				h. 2
2			bought a total of 18 Mathematics and Science textbooks during a sale. He lathematics textbooks.	
	(a)	Expr	ess the number of Science textbooks he bought in terms of y .	[1]
	The \$10.	cost of	f a Mathematics textbook was \$6 and the cost of a Science textbook was	
	(b)		e down and simplify an expression, in terms of y, for the total amount mond spent.	[2]
	(c)		n that the total amount Raymond spent was \$136, form an equation in y solve it to find the number of Mathematics textbooks he bought.	[2]
3	A sal	lesmar	n monthly wage, \$W, is based on the formula $W = B + 20C$,	
		e B is	the basic wage and C is the number of watches he sold in a month. In that the salesman received \$1250 for selling 28 watches in a particular	
	(a)	mont	th, find B. t does the number 20 in the formula represent?	[2] [1]
	(b)			
	(c)	If the	e salesman sold 45 watches in a month, find his monthly wage.	[1]

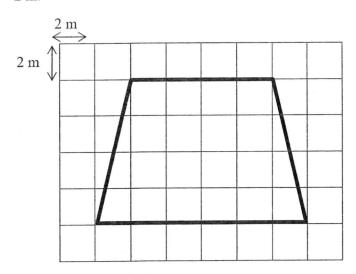
- 4 (a) Express $\frac{4x+3}{2} \frac{x-4}{5} + x$ as a single fraction in its simplest form. [3]
 - (b) Solve the equation $\frac{2}{3y-5} = \frac{3}{7-2y}.$ [3]
- In the diagram below, ABCDE forms part of a regular n-sided polygon. Two **equilateral** triangles, ΔBCP and ΔCDR , and a **square** CPQR are constructed along the side BCD of the polygon.



Find the number of sides, n, of the n-sided polygon.

[3]

6 Lisa has been tasked to create an eco-garden in her school with organic top soil. The diagram below shows the plan of the eco-garden whereby each square is 2 m by 2 m.



(a) Find the area of the eco-garden shown in the plan above.

[2]

Lisa was tasked to buy organic top soil to fill the eco-garden in her school. She saw this advertisement in the newspaper.

Value Packs	No. of kilograms per pack	Cost per kilogram
A	1 or 2	5.98
В	3 or 4	5.59
C	5 or 6	5.22

(b) To fill the eco-garden completely, Lisa needs 8 kg of organic top soil. Which **two** value packs should she buy such that it is **more cost-effective** for the school? Explain your recommendation with relevant working.

[3]

End of Paper

Check all your answers carefully!

Section A (50 marks)

- 1. (a) Round off 0.0749618 to 3 significant figures.
- Answer (a) 0.0750 [B1] [1]
- (b) Use a calculator to evaluate $\frac{\sqrt{42} \left(\frac{11}{3}\right)^2}{0.7\pi + \left(\sqrt[3]{151} (-2)^3\right)}$, giving your answer correct to 2 decimal places.

$$\frac{\sqrt{42} - \left(\frac{11}{3}\right)^2}{0.7\pi + \left(\sqrt[3]{151} - (-2)^3\right)} = -0.448571181$$
$$= -0.45 \text{ (correct to 2 dec. pl.)}$$

- Answer (b) <u>-0.45 [B1]</u> [1]
- 2. Without the use of a calculator, estimate the value of $\frac{17 \div \sqrt{93}}{\sqrt[3]{209} 4.58}$, giving your answer correct to 1 significant figure.

$$\frac{17 \div \sqrt{93}}{\sqrt[3]{209} - 4.58}$$

$$\approx \frac{20 \div \sqrt{100}}{\sqrt[3]{216} - 5}$$

$$= \frac{20 \div 10}{6 - 5}$$

$$= 2$$
[M1] 4 correct estimation

Answer 2 [2]

Study the set of numbers and write down all the irrational numbers in the answer space provided.

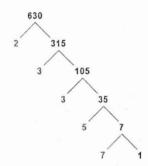
$$-0.33, -\frac{1}{7}, 0, \sqrt{169}, \pi, \sqrt{0.5}, \sqrt{8}, 1.3, 2^3$$

Answer $\pi, \sqrt{0.5}, \sqrt{8}$ [B1] [1]

4. Written as the product of its prime factors,

$$252 = 2^2 \times 3^2 \times 7.$$

(a) Express 630 as the product of its prime factors in index notation.



$$630 = 2 \times 3^2 \times 5 \times 7$$
 ---- [B1]

Answer (a)
$$630 = 2 \times 3^2 \times 5 \times 7$$
 [1]

(b) Find the HCF of 252 and 630. Give your answer as the product of its prime factors in index notation.

$$252 = 2^{2} \times 3^{2} \times 7$$

 $630 = 2 \times 3^{2} \times 5 \times 7$
 $HCF = 2 \times 3^{2} \times 7$ ---- [B1]

Answer (b)
$$2 \times 3^2 \times 7$$
 [1]

(c) Find the smallest possible value of a whole number x if 630x is a multiple of 252.

L.C.M =
$$2^2 \times 3^2 \times 5 \times 7$$
 ---- [M1]
 $630x = 2^2 \times 3^2 \times 5 \times 7$

$$x = \frac{2^2 \times 3^2 \times 5 \times 7}{2 \times 3^2 \times 5 \times 7}$$

$$x = 2$$
 ---- [A1]

Answer (c)
$$\underline{x} = \underline{2}$$
 [2]

5. Simplify the following expressions.

(a)
$$3(x-y)+[5x-(-2x+y)]$$

 $3(x-y)+[5x-(-2x+y)]$ ---- [M1] Expansion of " $-(-2x+y)$ "
 $=3(x-y)+(5x+2x-y)$
 $=3(x-y)+(7x-y)$
 $=3x-3y+7x-y$ ---- [M1] Expansion of " $3(x-y)$ "
 $=10x-4y$ ---- [A1]

Answer (a) 10x - 4y [3]

(b)
$$\frac{(x-2x^2)}{x} - 4x$$

$$= \frac{x(1-2x)}{x} - 4x$$

$$= \frac{x(1-2x)}{x(1)} - 4x$$

$$= 1 - 2x - 4x$$

$$= 1 - 6x$$
---- [A1]

Answer (b)
$$1-6x$$
 [2]

- 6. Factorise the following expressions completely
 - (a) 42ac 7c, 42ac - 7c = 7c(6a - 1) ---- [B1]

Answer (a)
$$\frac{7c(6a-1)}{6a-1}$$
 [1]

(b) $5x^2 - 10xy + 15x$.

$$5x^2 - 10xy + 15x = 5x(x - 2y + 3)$$
 --- [B1]

Answer (b)
$$5x(x-2y+3)$$
 [1]

- 7. Solve the following equations.
 - (a) 5k+4=-2(k-9)

$$5k + 4 = -2(k - 9)$$

 $5k + 4 = -2k + 18$ ---- [M1] Expansion of " $-2(k - 9)$ "
 $5k + 2k = 18 - 4$
 $7k = 14$

$$7k = 14$$

$$k = 2$$
---- [A1]

Answer (a)
$$\underline{k} = 2$$
 [2]

(b)
$$7-n = \frac{-9n+1}{2}$$

$$7-n = \frac{-9n+1}{2}$$

 $2(7-n) = -9n+1$ ---- [M1] Multiply both sides by 2
 $14-2n = -9n+1$ ---- [M1] Expansion of "2(7-n)"

$$14 - 2n = -9n + 1$$
$$-2n + 9n = 1 - 14$$

$$7n = -13$$

$$n = -1\frac{6}{7}$$
 --- [A1]

Answer (b)
$$n = -1\frac{6}{7}$$
 [3]

8. If
$$k = \sqrt{\frac{2m}{m-n}}$$
, find the value of *n* when $k = 2$ and $m = -4$.

$$k = \sqrt{\frac{2m}{m-n}}$$

$$2 = \sqrt{\frac{2(-4)}{-4-n}}$$
---- [M1] Substitution of correct values
$$2^2 = \frac{-8}{-4-n}$$

$$4(-4-n) = -8$$

$$-16-4n = -8$$

$$-4n = -8+16$$

$$-4n = 8$$

$$n = -2$$
---- [A1]

Answer
$$\underline{n=-2}$$
 [3]

9. George has \$y and Sam has \$18 more than George. Tim has half the total amount of George and Sam.

Find an expression, in terms of y, for

(a) the amount of money Sam has,

Sam has
$$(y + 18)$$
 ---- [B1]

Answer (a)
$$\$(y+18)$$
 [1]

(b) the total amount the 3 of them have together.

Amount of money Tim has

$$= \frac{1}{2}(y+y+18)$$

= \$(y+9) --- [M1]

Total amount
=
$$y + (y+18) + (y+9)$$

= $\$(3y+27)$ ---- [A1]

Answer (b)
$$\$(3y + 27)$$
 [2]

10. Without using a calculator and showing your working clearly, evaluate

$$\left(\frac{2}{3} + \frac{3}{4}\right) \times \left(\frac{4}{3} \div \frac{2}{3}\right).$$

$$\left(\frac{2}{3} + \frac{3}{4}\right) \times \left(\frac{4}{3} \div \frac{2}{3}\right)$$

$$= \left(\frac{8}{12} + \frac{9}{12}\right) \times \left(\frac{4}{3} \times \frac{3}{2}\right) \quad ---- \quad [M1] \text{ fractions with common denominator}$$

$$= \frac{17}{12} \times 2$$

$$= \frac{17}{6}$$

$$= 2\frac{5}{6} \qquad ---- \quad [A1]$$

Answer
$$2\frac{5}{6}$$
 [3]

- 11. The foot of the mountain is at sea level. The temperatures at the foot and at the summit of the mountain are 11° C and -7° C respectively.
 - (a) Find the difference between the two temperatures.

Difference between the two temperatures

$$=11-(-7)$$

$$=18^{\circ}C$$

(b) Suppose that the temperature drops by 6°C for every 1000 m above sea level. How high is the mountain above sea level?

Height of the mountain

$$=\frac{18}{6} \times 1000$$
 ---- [M1]

$$=3000 \text{ m}$$
 ---- [A1]

OR No. of times =
$$18 \div 6$$

= 3
Height of mountain = 3×1000 ---- [M1]
= 3000 m ---- [A1]

12.

WAFFLES

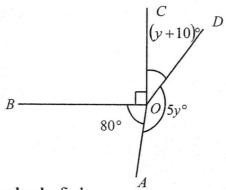
Write down all the letters in the word above that have

(a) one line of symmetry,

Answer (a) \underline{W} , \underline{A} , \underline{E} [B1] [1]

(b) rotational symmetry of order two.

- Answer (b) S [B1] [1]
- 13. In the figure below, OA, OB, OC and OD are all straight lines. $\angle COB = 90^{\circ}$ and $\angle AOB = 80^{\circ}$.



Stating your reasons clearly, find

(a) the value of y,

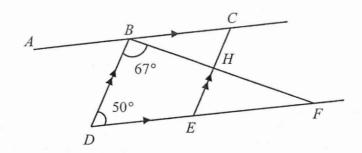
$$90 + 80 + 5y + y + 10 = 360$$
 (\angle s at a point) ---- [M1] O,P for missing/wrong
 $180 + 6y = 360$ reason
 $y = 30$ ---- [A1]

Answer (a)
$$y = 30$$
 [2]

(b) the obtuse angle
$$AOD$$
.
 $\angle AOD = 5(30)$
= 150° ---- [B1]

Answer (b)
$$150^{\circ}$$
 [1]

14. In the figure below, ABC, DEF and BHF are straight lines. AC // DF and BD // CE. $\angle DBF = 67^{\circ}$ and $\angle BDF = 50^{\circ}$.



Stating your reasons clearly, find

- (a) $\angle BCE$, $\angle BCE$ = 50° (opp. \angle s of //gram) ---- [B1] \bigcirc ,P for missing/wrong reason
 - Answer (a) 50° [1]
- (b) ∠ABD, ∠ABD

 = 50° (alt. ∠s, AC//DF) ---- [B1] ○,P for missing/wrong reason

 Or

 ∠ABD

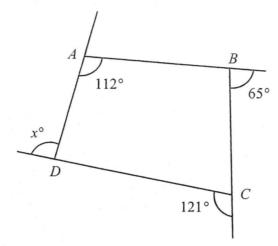
 = 50° (corr. ∠s, BD//CE)

Answer (b) 50° [1]

(c) $\angle CBH$. $\angle CBH$ = $180^{\circ} - 50^{\circ} - 67^{\circ}$ (adj. \angle s on a st. line) ---- [M1] \bigcirc , P for missing/wrong reason = 63° or (int. \angle s, BC//DE) ---- [A1]

Answer (c) <u>63°</u> [2]

15. In the diagram below, ABCD is a quadrilateral. $\angle DAB = 112^{\circ}$ while two of its exterior angles are 65° and 121° . Find the value of x.



$$x + (180-112) + 65 + 121 = 360$$
 (ext. \angle sum of polygon) ---- [M1] \bigcirc ,P for $x + 68 + 65 + 121 = 360$ missing/wrong $x = 360 - 284$ reason $x = 106$ ---- [A1]

OR

$$\angle ABC = 180^{\circ} - 65^{\circ}$$
 (adj. \angle s on a str. line)
 $= 115^{\circ}$
 $\angle BCD = 180^{\circ} - 121^{\circ}$ (adj. \angle s on a str. line)
 $= 59^{\circ}$
 $\angle ADC = 360^{\circ} - 115^{\circ} - 59^{\circ} - 112^{\circ}$ (\angle sum of quadrilateral)
 $= 74^{\circ}$
 $\angle x = 180^{\circ} - 74^{\circ}$ (adj. \angle s on a str. line) ---- [M1] \bigcirc , P for missing/wrong
 $= 106^{\circ}$ reason

Answer $\underline{x} = 106^{\circ}$ [2]

16. (a) In the answer space below, construct a triangle XYZ such that XY = 9 cm, YZ = 10 cm and ∠XYZ = 85°. The line XY has already been drawn. [3]
(b) On the same diagram,
(i) construct the angle bisector of ∠XZY. [1]
(ii) construct the perpendicular bisector of YZ. [1]
(c) The point M is the intersection of the two bisectors drawn. Measure and write

down the value of obtuse $\angle XMZ$.

Y 9 cm *Y*

[C3] - correct shape - YZ arc seen - ∠XYZ measured

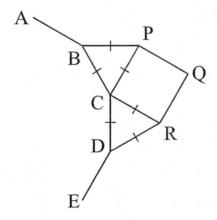
Answer (c) $\angle XMZ = \underline{144}^{\circ}$ [1]

Section B (30 marks)

Answer all the questions in this section on the writing paper provided.

1	(a)	A rec	etangular board measures 198 cm by 156 cm. It is cut into squares of equal with no material left over.	
		Find (i) (ii)	the largest possible length of the side of the square, the largest possible area of such a square.	[2] [1]
		(iii)	the number of squares formed.	[1]
	(b)	years	different comets pass through our solar system every 64 years and 216 respectively. The last time they passed through our solar system together a the year 2014. In which year will they next pass through our solar system ner?	[3]
2	Rayr	nond be	ought a total of 18 Mathematics and Science textbooks during a sale. He athematics textbooks.	
	(a)	Expre	ss the number of Science textbooks he bought in terms of y.	[1]
	The 6 \$10.		a Mathematics textbook was \$6 and the cost of a Science textbook was	
	(b) (c)	Kaym	down and simplify an expression, in terms of y, for the total amount ond spent. that the total amount Raymond spent was \$136, form an equation in y	[2]
		and so	elve it to find the number of Mathematics textbooks he bought.	[2]
3	A sal	esman	monthly wage, \$W, is based on the formula $W = B + 20C$,	
	where (a)	Given	the basic wage and C is the number of watches he sold in a month. that the salesman received \$1250 for selling 28 watches in a particular	
	(b)	month	, find B. does the number 20 in the formula represent?	[2] [1]
	(c)	If the s	salesman sold 45 watches in a month, find his monthly wage.	[1]

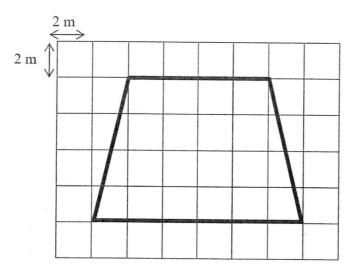
- 4 (a) Express $\frac{4x+3}{2} \frac{x-4}{5} + x$ as a single fraction in its simplest form. [3]
 - (b) Solve the equation $\frac{2}{3y-5} = \frac{3}{7-2y}.$ [3]
- In the diagram below, ABCDE forms part of a regular n-sided polygon. Two **equilateral** triangles, ΔBCP and ΔCDR , and a **square** CPQR are constructed along the side BCD of the polygon.



Find the number of sides, n, of the n-sided polygon.

[3]

6 Lisa has been tasked to create an eco-garden in her school with organic top soil. The diagram below shows the plan of the eco-garden whereby each square is 2 m by 2 m.



(a) Find the area of the eco-garden shown in the plan above.

[2]

Lisa was tasked to buy organic top soil to fill the eco-garden in her school. She saw this advertisement in the newspaper.

Value Packs	No. of kilograms per pack	Cost per kilogram	
A	1 or 2	5.98	
В	3 or 4	5.59	
С	5 or 6	5.22	

(b) To fill the eco-garden completely, Lisa needs 8 kg of organic top soil. Which **two** value packs should she buy such that it is **more cost-effective** for the school? Explain your recommendation with relevant working.

[3]

End of Paper Check all your answers carefully!

MID-YEAR EXAMINATIONS (SEC 1E) ANSWER KEY

Section	n A	Sectio	n B
la	0.0750	lai	6 cm
ь	-0.45	aii	36 cm ²
2	2	aiii	858
3	$\pi, \sqrt{0.5}, \sqrt{8}$	b	3742
4a	$630 = 2 \times 3^2 \times 5 \times 7$	2a	(18-y)
b	$2\times3^2\times7$	b	(-4y+180)
С	x = 2	С	11
5a	10x-4y	3a	\$690
b	1 – 6 <i>x</i>	b	The number 20 represent the commission/extra money he will receive with every watch sold.
6a	7c(6a-1)	С	\$1590
b	7c(6a-1) $5x(x-2y+3)$	4a	$\frac{28x + 23}{10}$
7a	<i>k</i> = 2	b	$y = 2\frac{3}{13}$
b	$-1\frac{6}{7}$	5	12
8	n = -2	6a	80 m ²
9a	\$(y + 18)	b	Lisa needs to buy 5 kg of Value Pack C organic soil and 3 kg of Value Pack B organic soil to make up of 8 kg of organic top soil. The lowest cost that she can get is \$42.87.
b	(3y + 27)		
10	$2\frac{5}{6}$		
l la	18°C		
ь	3000 m		
12a	W, A, E		
b	S		
13a	y = 30		
ь	150°		
14a	50°		
b	50°		
С	63°		
15	x = 106°		
16c	144°		